# Leveraging Ensemble Diversity for Robust Self-Training under Sample Selection Bias

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MLSP seminar, ENS Lyon

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### Outline



- 1 Introduction
- 2 Failure of Self-Training
- ${\bf 3}$  Learning with the  ${\cal T}$ -similarity
- **4** Numerical Experiments
- 6 Discussion

## Outline

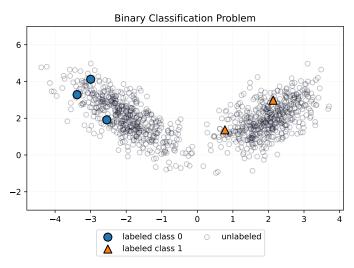


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#### Introduction



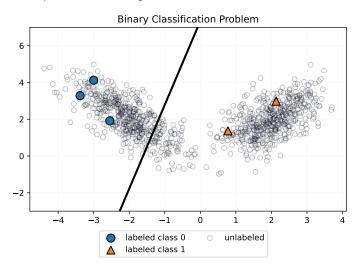
In some applications, data acquisition is cheaper than labeling ...



#### Introduction



... and supervised learning is inefficient.



# Semi-Supervised Learning (SSL)



 $\mathsf{SSL} \to \mathsf{learn}$  from a few labeled and many unlabeled examples.



# Semi-Supervised Learning (SSL)



 $SSL \rightarrow$  learn from a few labeled and many unlabeled examples.



#### Families of SSL Methods



- ★ Pseudo-labeling (Amini et al., 2023):
  - Unlabeled regularization (Feofanov et al., 2023)
  - Self-training (Feofanov et al., 2019)
- \* Graph-based algorithms (van Engelen and Hoos, 2020):
  - Label propagation
  - Label spreading
- \* Unsupervised preprocessing (van Engelen and Hoos, 2020):
  - Cluster-then-label
  - Feature extraction: auto-encoders, PCA
  - Pre-training: self-supervised learning, stacked auto-encoders

#### Families of SSL Methods

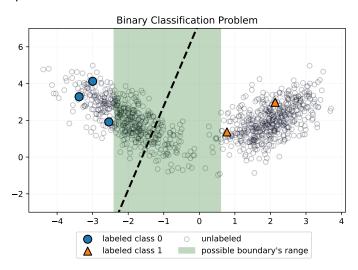


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## Low Density Separation



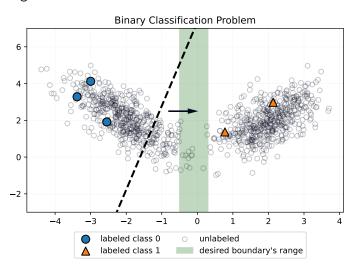
Range of possible supervised classifiers is vast: we need to make assumptions.



# Low Density Separation



Low Density Separation (LDS) assumption: push boundary away from regions of unlabeled data.



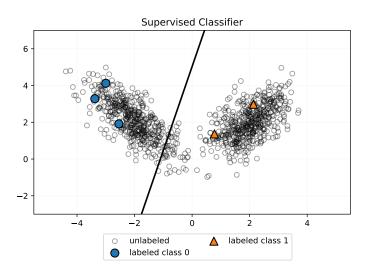
## Family of SSL Methods



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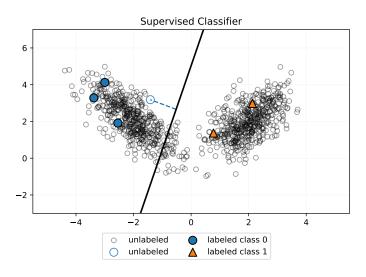


Start from a supervised classifier trained on the labeled set.



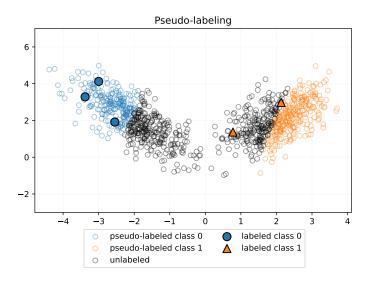


Predict labels and confidence scores for unlabeled data.





Pseudo-label most confident data and include in the labeled set.





Retrain the model and repeat the same procedure again.





And again...



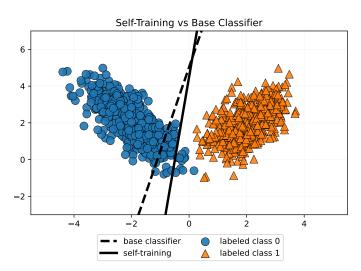


Until there are no data to pseudo-label.





Self-training pushed the boundary away from the confident data.



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 $\star$  Confidence Estimation  $\to$  How to rank unlabeled data?

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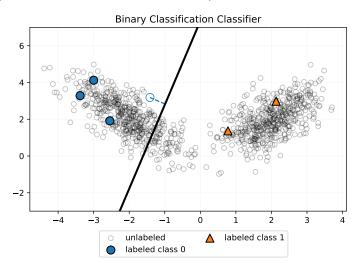
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In this work, we focus on Confidence Estimation.

#### Failure Cases



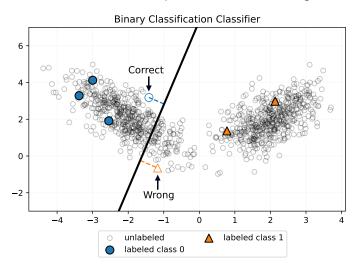
Requirements  $\rightarrow$  trust the classifier's predictions.



#### Failure Cases



Problem  $\rightarrow$  not safe since the prediction can be wrong.

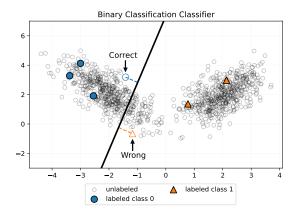


#### Failure Cases



Biased prediction confidence  $\Rightarrow$  wrong direction can be chosen.

 $\rightarrow$  This can occur when there is a distribution shift in the data.





- \* SSL assumption: labeled and unlabeled data are i.i.d.
- $\star$  Confidence can be biased when this assumption does not hold



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- Sample Selection Bias (SSB): data labeling subject to constraints
  - Creation of group study in clinical trials;
  - People with poor mobility less likely to be in street surveys;
  - Labeling can be constrained for privacy reasons.



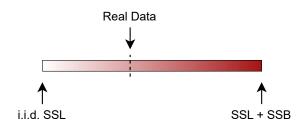
- \* SSL assumption: labeled and unlabeled data are i.i.d.
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- Sample Selection Bias (SSB): data labeling subject to constraints
  - Creation of group study in clinical trials;
  - People with poor mobility less likely to be in street surveys;
  - Labeling can be constrained for privacy reasons.
- \* SSB has been studied but not in the case of SSL.

# SSL under Sample Selection Bias



SSL + SSB combines SSL and Sample Selection Bias (SSB):

- Few labeled examples (SSL)
- ② Biased labeling procedure (SSB)



Goal  $\rightarrow$  obtain a method good on **both** i.i.d. SSL and SSL + SSB.

# Implementation of SSL + SSB



#### Select the labeled set to violate the i.i.d. assumption.

- Binary selection variable  $s_i$  for each  $\mathbf{x}_i$ ;
- $s_i = 1$  if  $\mathbf{x}_i$  is labeled,  $s_i = 0$  otherwise;
- Model  $\mathbb{P}(s_i = 1 | \mathbf{x}_i, y_i)$  to violate i.i.d. assumption.

# Implementation of SSL + SSB



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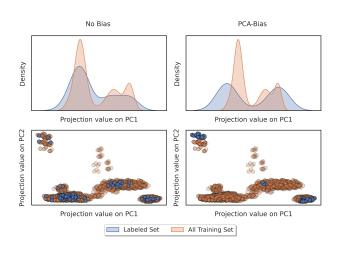
PCA-Bias  $\rightarrow$  for each class c,

- **1** Apply PCA on training data of class c;
- **2** Compute  $proj_1(\mathbf{x}_i)$ , projection value on PC1;

## Implementation of SSL + SSB



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# Pseudo-Labeling Policies



- \* ERM corresponds to supervised learning on the labeled set
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# Failure of Self-Training under SSL + SSB



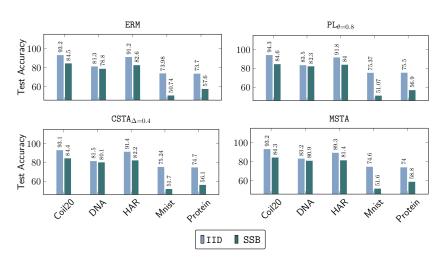


Figure: Test accuracies of the different baselines on 5 datasets. Full results to be found here.

#### Unreliable Model Selection



#### LOO over-optimistic w.r.t. generalization performance (Figure 1).

- Leave one labeled point out;
- Train on the remaining  $n_{\ell}-1$ ;
- Test on the one left out;
- Repeat for each labeled point.

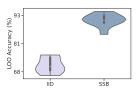


Figure: LOO on Mnist.

#### Outline



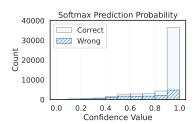
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#### Motivation



softmax-based confidence measure is unreliable in SSL + SSB.

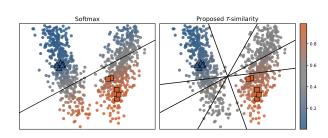
- NNs are overconfident;
- softmax predictions biased towards the labeled set.



 $\rightarrow$  We propose a novel confidence measure for NNs.

# Leveraging Ensemble Diversity

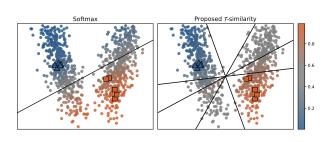




$$\min_{\mathcal{T}} \frac{1}{M} \sum_{h \in \mathcal{T}} \underbrace{\left(\frac{1}{n_{\ell}} \sum_{(\mathbf{x}, y) \in \mathbf{X}_{\ell} \times \mathbf{y}_{\ell}} \ell(h(\mathbf{x}), y)\right)}_{\text{supervised loss}} + \underbrace{\frac{\gamma}{n_{u} M (M-1)} \sum_{h \neq \tilde{h} \in \mathcal{T}} \sum_{\mathbf{x} \in \mathbf{X}_{u}} h(\mathbf{x})^{\top} \tilde{h}(\mathbf{x})}_{\text{agreement loss}}$$

# Leveraging Ensemble Diversity





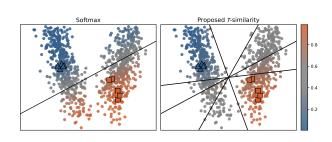
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We jointly train the ensemble to

- 1 Fit very well the labeled data
- 2 Disagree as much as possible on unlabeled data

# Leveraging Ensemble Diversity





$$\min_{\mathcal{T}} \frac{1}{M} \sum_{h \in \mathcal{T}} \underbrace{\left(\frac{1}{n_{\ell}} \sum_{(\mathbf{x}, y) \in \mathbf{X}_{\ell} \times \mathbf{y}_{\ell}} \ell(h(\mathbf{x}), y)\right)}_{\text{supervised loss}} + \underbrace{\frac{\gamma}{n_{u} M (M - 1)} \sum_{h \neq \tilde{h} \in \mathcal{T}} \sum_{\mathbf{x} \in \mathbf{X}_{u}} h(\mathbf{x})^{\top} \tilde{h}(\mathbf{x})}_{\text{agreement loss}}$$

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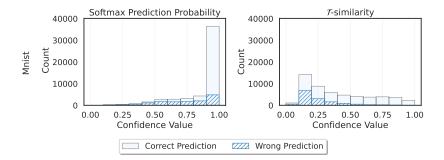
## $\mathcal{T}$ -similarity



 $\star$  We define the  $\mathcal{T}$ -similarity as:

$$s_{\mathcal{T}}(\mathbf{x}) = \frac{1}{M(M-1)} \sum_{h \neq \tilde{h} \in \mathcal{T}} h(\mathbf{x})^{\top} \tilde{h}(\mathbf{x}).$$

\* For any  $\mathbf{x}$ , we have  $0 \leq s_{\mathcal{T}}(\mathbf{x}) \leq 1$ .



## Practical Implementation



- Projection layers are learned through a classification head;
- **2** Confidence estimator is ensemble of  $M\!=\!5$  linear heads that don't affect representation.

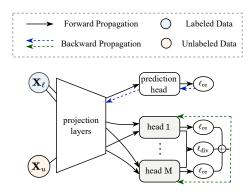


Figure: Architecture of the model.

# Binary Linear Case



- Fixed representation of dimension d, binary linear classification
- Linear ensemble  $\mathbf{W} = \{ \boldsymbol{w}_m \in \mathbb{R}^d | 1 \le m \le M \}$
- Prediction of  $oldsymbol{\omega}_m$  on  $\mathbf{x}$  is  $\mathrm{sign}(oldsymbol{\omega}_m^{ op}\mathbf{x})$

$$\underset{\mathbf{W} \in \mathbb{R}^{d \times M}}{\operatorname{argmin}} \mathcal{L}(\mathbf{W}) \coloneqq \underbrace{\frac{1}{Mn_{\ell}} \sum_{m=1}^{M} \sum_{i=1}^{n_{\ell}} \left( y_{i} - \boldsymbol{\omega}_{m}^{\top} \mathbf{x}_{i} \right)^{2} + \underbrace{\frac{1}{M} \sum_{m=1}^{M} \lambda_{m} \|\boldsymbol{\omega}_{m}\|^{2}}_{\text{regularization}} + \underbrace{\frac{\gamma}{n_{u} M(M-1)} \sum_{m \neq k} \sum_{i=n_{\ell}+1}^{n_{\ell}+n_{u}} w_{m}^{\top} \mathbf{x}_{i} w_{k}^{\top} \mathbf{x}_{i}}_{\text{agreement term}},$$

$$(\mathbf{P})$$

where  $\gamma$  controls the influence of the diversity on the learning.

# Convergence to a Stationary Point



- Labeled set  $(\mathbf{X}_\ell, \mathbf{y}_\ell) = (\mathbf{x}_i, y_i)_{i=1}^{n_\ell}$
- Unlabeled set  $\mathbf{X}_u = (\mathbf{x}_i)_{i=n_\ell+1}^{n_\ell+n_u}$
- Assumption:

$$\forall m \in [1, M], \lambda_m > \frac{\gamma(M+1)}{n_u(M-1)} \lambda_{max}(\mathbf{X}_u^\top \mathbf{X}_u)$$
 (A)

#### Theorem (O., Feofanov, Redko)

Under Assumption A,  $\mathcal{L}$  is strictly convex and coercive on  $\mathbb{R}^{d\times M}$ . Hence, the optimization problem (P) admits a unique solution  $\mathbf{W}^*$  that verifies

$$\nabla \mathcal{L}(\mathbf{W}^*) = 0. \tag{1}$$

# Diversity of an Ensemble



$$\ell_{\mathsf{div}}(\mathbf{W}, \mathbf{X}_u) \!=\! -\frac{1}{n_u M (M-1)} \sum_{m \neq k} \boldsymbol{\omega}_m^\top \mathbf{X}_u^\top \mathbf{X}_u \boldsymbol{\omega}_k.$$

#### Theorem (O., Feofanov, Redko)

$$\gamma \ell_{div}(\mathbf{W}^*, \mathbf{X}_u) \ge \frac{1}{2n_{\ell}M} \sum_{m=1}^{M} \|\mathbf{y}_{\ell} - \mathbf{X}_{\ell} \boldsymbol{\omega}_m^*\|_2^2$$
$$+ \frac{1}{2M} \sum_{m=1}^{M} (\boldsymbol{\omega}_m^*)^{\top} \left( \lambda_m \mathbf{I}_d + \frac{\mathbf{X}_{\ell}^{\top} \mathbf{X}_{\ell}}{n_{\ell}} \right) \boldsymbol{\omega}_m^*.$$

- 1 Trade-off between supervised performance and margin term
- 2 Assuming orthogonality, the predictors  $\omega_m$  span the M directions of largest variance of the labeled data.

# Diversity of an Ensemble



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#### Theorem (O., Feofanov, Redko)

$$\gamma \ell_{\textit{div}}(\mathbf{W}^*, \mathbf{X}_u) \geq \frac{1}{2M} \bigg( \lambda + \frac{1}{n_\ell} \lambda_{\min} \left( \mathbf{X}_\ell^\top \mathbf{X}_\ell \right) \bigg) \|\mathbf{W}^*\|_F^2.$$

- 1 Direction of smallest variance is also important for diversity
- Theorem shows the importance of representation learning

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## Diversity provides Calibrated Confidence Measure



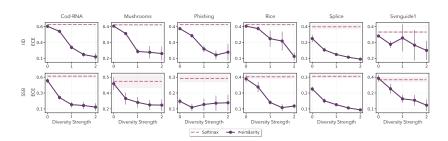


Figure: Increasing the diversity improves the classifier's calibration

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# Results in SSL+SSB



Dataset	ERM	$PL_{\theta=0.8}$		$\mathtt{CSTA}_{\Delta=0.4}$		MSTA	
Butaset		softmax	$\mathcal{T}$ -similarity	softmax	$\mathcal{T}$ -similarity	softmax	$\mathcal{T}$ -similarity
Cod-RNA	$74.51 \pm 8.86$	$74.75 \pm 8.14$	$80.06 \pm 3.55$	$73.39 \pm 7.36$	$78.39 \pm 4.66$	$75.28 \pm 8.79$	$\textbf{76.88} \pm \textbf{7.67}$
COIL-20	$84.54 \pm 2.19$	$84.69 \pm 3.56$	$84.57 \pm 2.85$	$84.38 \pm 3.05$	$84.57 \pm 3.16$	$84.32 \pm 2.34$	$84.07 \pm 2.85$
Digits	$75.68 \pm 4.59$	$80.47 \pm 3.8$	$78.2 \pm 3.34$	$78.4 \pm 3.28$	$\textbf{79.14} \pm \textbf{3.5}$	$78.02 \pm 5.15$	$79.8 \pm 5.92$
DNA	$78.82 \pm 2.31$	$80.29 \pm 2.24$	$79.06 \pm 2.31$	$80.12 \pm 2.08$	$80.76 \pm 2.24$	$80.89 \pm 2.64$	$84.09 \pm 1.7$
DryBean	$64.6 \pm 3.89$	$65.6 \pm 4.18$	$61.55 \pm 4.91$	$64.91 \pm 3.72$	$64.6 \pm 3.53$	$66.24 \pm 4.31$	$67.0 \pm 3.96$
HAR	$82.57 \pm 1.96$	$82.87 \pm 3.02$	$83.12 \pm 2.27$	$82.19 \pm 2.61$	$83.53 \pm 3.77$	$81.35 \pm 2.54$	$81.16 \pm 1.63$
Mnist	$50.74 \pm 2.25$	$51.08 \pm 2.55$	$52.69 \pm 2.42$	$51.7 \pm 3.52$	$54.26 \pm 1.82$	$51.6 \pm 2.58$	$54.18 \pm 2.34$
Mushrooms	$69.45 \pm 7.29$	$59.53 \pm 10.46$	$71.36 \pm 6.63$	$62.98 \pm 7.25$	$77.55 \pm 7.65$	$72.16 \pm 7.59$	$76.16 \pm 13.04$
Phishing	$67.42 \pm 3.55$	$66.08 \pm 5.66$	$\textbf{77.41} \pm \textbf{3.93}$	$66.88 \pm 5.64$	$76.17 \pm 8.58$	$69.48 \pm 4.37$	$\textbf{75.83} \pm \textbf{7.52}$
Protein	$57.57 \pm 6.33$	$57.45 \pm 6.36$	$57.61 \pm 6.23$	$56.09 \pm 5.61$	$57.74 \pm 7.8$	$58.81 \pm 6.54$	$59.88 \pm 6.29$
Rice	$79.19 \pm 5.12$	$80.54 \pm 4.31$	$81.1 \pm 4.28$	$79.88 \pm 4.48$	$81.56 \pm 3.61$	$80.35 \pm 4.89$	$82.63 \pm 5.63$
Splice	$66.13 \pm 4.47$	$67.14 \pm 2.62$	$67.45 \pm 2.53$	$67.28 \pm 2.07$	$68.05 \pm 2.17$	$66.08 \pm 4.98$	$66.32 \pm 4.73$
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- ★ Mushrooms and Phishing → from degradation to improvement;

#### Results in SSL+SSB



Dataset	ERM	$PL_{\theta=0.8}$		$\mathtt{CSTA}_{\Delta=0.4}$		MSTA	
Buttaset		softmax	$\mathcal{T}$ -similarity	softmax	$\mathcal{T}$ -similarity	softmax	$\mathcal{T}$ -similarity
Cod-RNA	$74.51 \pm 8.86$	$74.75 \pm 8.14$	$80.06 \pm 3.55$	$73.39 \pm 7.36$	$78.39 \pm 4.66$	$75.28 \pm 8.79$	$\textbf{76.88} \pm \textbf{7.67}$
COIL-20	$84.54 \pm 2.19$	$84.69 \pm 3.56$	$84.57 \pm 2.85$	$84.38 \pm 3.05$	$84.57 \pm 3.16$	$84.32 \pm 2.34$	$84.07 \pm 2.85$
Digits	$75.68 \pm 4.59$	$80.47 \pm 3.8$	$78.2 \pm 3.34$	$78.4 \pm 3.28$	$\textbf{79.14} \pm \textbf{3.5}$	$78.02 \pm 5.15$	$79.8 \pm 5.92$
DNA	$78.82 \pm 2.31$	$80.29 \pm 2.24$	$79.06 \pm 2.31$	$80.12 \pm 2.08$	$80.76 \pm 2.24$	$80.89 \pm 2.64$	$84.09 \pm 1.7$
DryBean	$64.6 \pm 3.89$	$65.6 \pm 4.18$	$61.55 \pm 4.91$	$64.91 \pm 3.72$	$64.6 \pm 3.53$	$66.24 \pm 4.31$	$67.0 \pm 3.96$
HAR	$82.57 \pm 1.96$	$82.87 \pm 3.02$	$83.12 \pm 2.27$	$82.19 \pm 2.61$	$83.53 \pm 3.77$	$81.35 \pm 2.54$	$81.16 \pm 1.63$
Mnist	$50.74 \pm 2.25$	$51.08 \pm 2.55$	$52.69 \pm 2.42$	$51.7 \pm 3.52$	$54.26 \pm 1.82$	$51.6 \pm 2.58$	$54.18 \pm 2.34$
Mushrooms	$69.45 \pm 7.29$	$59.53 \pm 10.46$	$71.36 \pm 6.63$	$62.98 \pm 7.25$	$77.55 \pm 7.65$	$72.16 \pm 7.59$	$76.16 \pm 13.04$
Phishing	$67.42 \pm 3.55$	$66.08 \pm 5.66$	$77.41 \pm 3.93$	$66.88 \pm 5.64$	$\textbf{76.17} \pm \textbf{8.58}$	$69.48 \pm 4.37$	$75.83 \pm 7.52$
Protein	$57.57 \pm 6.33$	$57.45 \pm 6.36$	$57.61 \pm 6.23$	$56.09 \pm 5.61$	$\textbf{57.74} \pm \textbf{7.8}$	$58.81 \pm 6.54$	$59.88 \pm 6.29$
Rice	$79.19 \pm 5.12$	$80.54 \pm 4.31$	$81.1 \pm 4.28$	$79.88 \pm 4.48$	$81.56 \pm 3.61$	$80.35 \pm 4.89$	$82.63 \pm 5.63$
Splice	$66.13 \pm 4.47$	$67.14 \pm 2.62$	$67.45 \pm 2.53$	$67.28 \pm 2.07$	$68.05 \pm 2.17$	$66.08 \pm 4.98$	$66.32 \pm 4.73$
Svmguide1	$70.89 \pm 10.98$	$70.35 \pm 11.74$	$81.07 \pm 5.39$	$69.84 \pm 11.06$	$74.46 \pm 7.23$	$71.04 \pm 11.11$	$\textbf{73.13} \pm \textbf{8.82}$

- $\star$   $\mathcal{T}$ -similarity is better overall;
- $\star$  Mushrooms and Phishing  $\to$  from degradation to improvement.
- ★ Results in i.i.d. SSL: no significant improvement nor degradation.

#### Outline



- Introduction
- Pailure of Self-Training
- ${f 3}$  Learning with the  ${\cal T}$ -similarity
- 4 Numerical Experiments
- Discussion

#### Discussion



- $\star$  Practical and principled framework to study SSL + SSB;
- \* Calibrated confidence measure;
- $\star$   $\,\mathcal{T}\text{-similarity}$  good both in i.i.d. SSL and SSL + SSB.

Future work  $\to$  use  $\mathcal{T}\text{-similarity}$  for iterative self-training, domain adaptation, or uncertainty modeling.

#### To Know More



This work has been accepted to AISTATS 2024, Valencia, Spain. You may find the links to the paper and the code below. to know more about my research, see my website: ambroiseodt.github.io and feel free to contact me.

```
* Paper: https://arxiv.org/abs/2310.14814
```

\* Code: https://github.com/ambroiseodt/tsim

# Acknowledgement

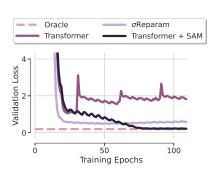


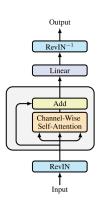
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#### Self-Promotion



# SAMformer: Unlocking the Potential of Transformers in Time Series Forecasting - Oral ICML 2024





- \* Paper: https://arxiv.org/pdf/2402.10198
- \* Code: https://github.com/romilbert/samformer

# Thanks for your attention!

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# Appendix: Datasets



Dataset	Size	$\#$ of lab. examples $n_\ell$	Dimension $d$	# classes $C$
Cod-RNA	59535	99	8	2
COIL-20	1440	200	1024	20
Digits	1797	99	64	10
DNA	3186	149	180	6
DryBean	13543	104	16	7
HAR	10299	299	561	3
Mnist	70000	100	784	10
Mushrooms	8124	79	112	2
Phishing	11055	99	68	2
Protein	1080	80	77	8
Rice	3810	29	7	2
Splice	3175	39	20	2
Svgmguide1	3089	39	4	2

Table: Characteristics of datasets used in our experiments